# **Virtual Physics**

## 16.12.2014

## **Exercise 11: Integration Methods**

#### Task 1: (from Exam WS 2010/2011)

Below you find the Butcher Tableau of an RK method of  $3^{rd}$  order.

0	0	0	0
1/3	1/3	0	0
2/3	0	2/3	0
1	1/4	0	3/4

Perform one integration step of this method on the following system!

 $dx/dt = -x^2 - 2 + 3t$ 

Start at t=0 with  $x_{t=0} = 1$ . The step-size h is 1.

Return the result for  $x_{t=1}$  as well as for the two sub-steps

Compute with rational numbers.

#### Task 2: (from Exam WS 2011/2012)

Below you find the coefficients for the BDF methods of different orders.

	$\alpha_{t+h}$	$\alpha_t$	$\alpha_{t-h}$	$\alpha_{t-2h}$	$\alpha_{t-3h}$
BDF 1	1	-1			
BDF 2	3/2	-2	1/2		
BDF 3	11/6	-3	3/2	-1/3	
BDF 4	25/12	-4	3	-4/3	1/4

Perform 3 integration steps of the highest applicable BDF method on the following system!

dx/dt = 2x - t + 1

Start at t=0 with  $x_{t=0}$  = -1. The step-size h is 1.

Return the result for  $x_{t=1}$ ,  $x_{t=2}$ , and  $x_{t=3}$ .

Compute with rational numbers.