# **Virtual Physics**

## 18.11.2014

## **Exercise 5: Tearing Algebraic Loops within an electric circuit**



## **Solution**

#### Task A: Set up the model equations

We select the 6 currents and 5 voltage potentials as selected above. Additionally, we introduce uC as voltage across the capacitor. This yields 12 variables in total.

There are 3 node equations for the corrent:

i1 = i2+i3

i4+i5 = i1

i4+i5+i6 = i2+i3

The remaining 9 equations result from the components.

i3 = I0 vS - vG = i2\*R2 vR - vS = i1\*R0 vC - vR = i1\*R3 vI-vC = uC der(uC)\*C = i1; der(i4)\*I = vI-vG vG-vI = R1\*i5 vG = 0;

#### Task B: Identify suitable tearing variables

uC and i4 are potential state variables and can assumed to be known.

Still only one two equations can be causalized:

i3 := I0;

vG := 0;

To continue, we select a tearing variable. i1 seems to be a good choice. It occurs in many equations and causalizes plenty of them.

#### i1 := iteration variable

vS := i2\*R2 + vG

vR := i1\*R0 + vS

vC := i1\*R3 + vR

vI := vC + uC;

i5 := i1 – i4;

#### residual := vG-vI - R1\*i5

der(uC) := i1/C;

der(i4) := (vI - vG)/I

i6 := i2 + i3 - i4 -i5

Remark: the equations der(i4) := (vI - vG)/I and der(uC) := i1/C are not part of the algebraic loop since the are not required for the computation of the residual.

i3	vG	i2	vS	vR	vC	vl	i5	i1	duC/ dt	di4/ dt	i6
Х											
	Х										
Х		Х						Х			
	Х		Х					Х			
			Х	Х				Х			
				Х	Х			Х			
					Х	Х					
							Х	Х			
	Х					Х	Х				
								X	X		
	Х					Х				Х	
Х		Х					Х				Х

This is the corresponding BLT form of the system:

Residual equations may lead to empty elements on the diagonal.